

RECONSTRUCTION OF CHAOTIC ATTRACTOR THROUGH FREESCALE DIGITAL SIGNAL PROCESOR

Ing. Jiří HNÍZDIL, Doctoral Degree Programme (2)
Dept. of Power Electrical and Electronic Engineering, FEEC, BUT
E-mail: xhnizd00@stud.feec.vutbr.cz

Ing. Jan NOVOTNÝ, Doctoral Degree Programme (1)
Dept. of Power Electrical and Electronic Engineering, FEEC, BUT
E-mail: xnovot40@stud.feec.vutbr.cz

Supervised by: Dr. Josef Koláčný

ABSTRACT

This article deals with reconstructing chaotic attractor through Freescale digital signal processor 56800 family. System is designed for use in the mechatronics applications for simulating dynamic's states of prosthetic's knuckle. Conception of project fully supplants chaotic analog circuits.

1 INTRODUCTION

Every system in the nature has an attractor. Attractor is a steady state of any state variables in the space. It can be for example steady velocity of motor shaft, steady trajectory of the Moon around the Earth and so on.

We know this types of attractors:

- Attractor is a fixed points
- Attractor is a periodic points
- Attractor is a kvaziperiodic points
- Chaotic attractor
- Strange attractor

Visualization of attractors creates different diagrams for example visualization of chaotic attractor give pictures called as a fractals. Fractals can be used in computer graphics as a textures, in the nature – for example structure of fern leaf. We implement fractal geometry into digital signal processor.

For more informations about attractors see some books which are listed on the end of this paper in references chapter.

2 MAIN PART

Chaotic system can be represented through two different electrical circuits:

2.1 CIRCUITS WITH ANALOG DEVICES

In this case, circuit is created through analog operation amplifier with nonlinear components in the feed forward loop. Classic schematic circuit which represents chaotic behavior is shown below on the figure no.1

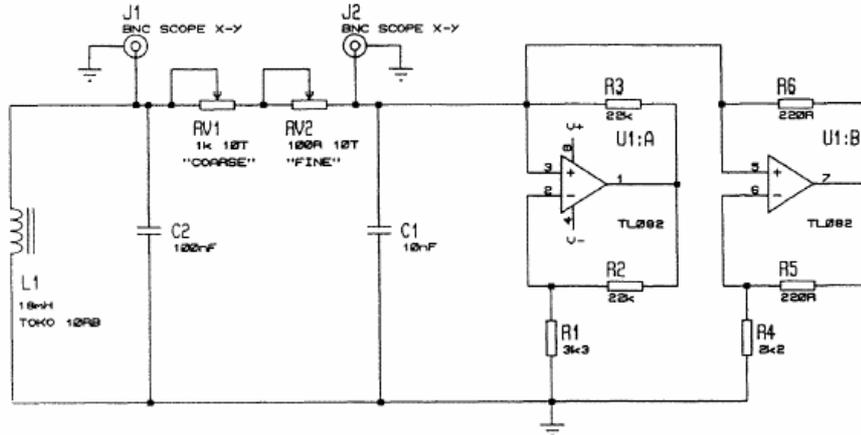


Fig. 1: Circuit diagram of analog chaotic system

Epitome of analog chaotic integrated device is for example Yamakawa's Lab & FLSI Chaos chip.

2.2 CIRCUITS WITH DIGITAL DEVICES

In this case, chaotic behavior is represented by means of mathematical algorithm stored in the microprocessor. This algorithm generates numbers and these numbers are converted by digital analog converter. Circuit diagram is shown below on the figure no.2

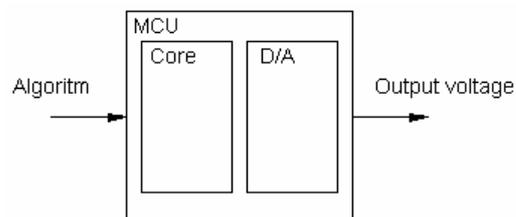


Fig. 2: Digital representation of chaos system

3 DESIGN

Freescale digital signal processor 56800 was used to develop system with chaotic

attractor. Math representation of chaotic attractor was stored in the DSP system memory, where run into iteration cycle.

Used math model is created by these equations:

For x axis:

$$x_n = \sin(y_{n-1} - b) + c \sin(x_{n-1} - b)$$

For y axis:

$$y_n = \sin(y_{n-1} - a) + c \sin(y_{n-1} - b)$$

Where

- a,b Initial conditions
- x_n, y_n present iteration step x and y axes position
- x_{n-1}, y_{n-1} previous iteration step x and y axes position

Outputs from digital to analog converters was connected to aritma 2d plotting system with prothetic knuckle. Frescale evolution board with dsp and aritma 2d plotting system are shown bellow on the figure no.3



Fig. 3: Evolution dsp board with 2d plotting system and scope

Used math algorithm is very sensitive on the initial conditions change. Some records of chaotic attractor are shown on the figures bellow in the result chapter. Type of reconstructed chaotic attractor is called as King’s dream fractal.

4 RESULTS

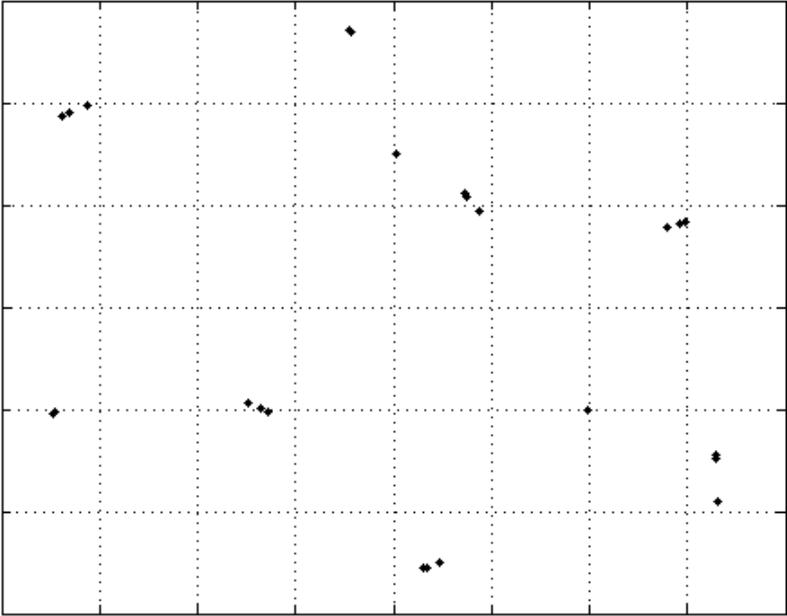


Fig. 4: Chaotic system with different initial variables set no. 1

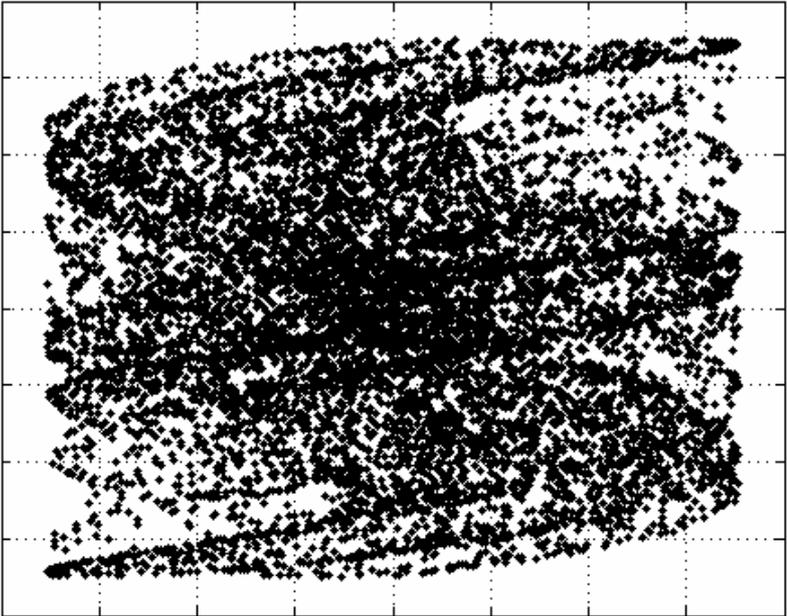


Fig. 5: Chaotic system with different initial variables set no. 2



Fig. 6: *Chaotic system with different initial variables set no. 3*

5 CONCLUSION

We created machatronic's aplication with digital signal procesor which one can be used for simulating dynamics states of prothetics knuckle. All of results are listed in the paper.

ACKNOWLEDGEMENTS

The paper has been prepared as a part of the solution of FRVŠ project No. 705/2005

REFERENCES

- [1] Chaos in Wonderland: Visual Adventures in a Fractal World, Palgrave Macmillan; Reprint edition (November 1, 1995), ISBN: 031212774X
- [2] <http://www.freescale.com>, 2005
- [3] http://www.vood.mysteria.cz/fraktaly/clanky/2.htm#tth_sEc1.2.4, 2005
- [4] <http://ej.iop.org/links/q98>, 2005